Advanced Microeconomics: Lecture Note 2

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1 Introduction of adverse selection/hidden characteristic

1 There are many choice situations where a principal delegates the completion of a task to an agent. Delegation can be motivated:

- either by the possibility of benefitting from some increasing returns associated with the division of tasks,

  劳动分工带来的报酬递增

  – e.g., the manager will be the only one to know the business conditions.

- or by the principal's lack of time or lack of any ability to perform the task himself,

  委托人没有时间或没有能力独立完成任务

  – e.g., the attorney knows better than the client how difficult the case will be.

- or by any other form of the principal's bounded rationality when facing complex problems.

  委托人在面临复杂问题时受到各种形式的有限理性约束

  – e.g., the tenant will be the only one to observe the exact local weather conditions.

2 By the mere fact of this delegation, the agent may get access to information that is not available to the principal.

In other words, the agent may have or gain private information, which is hidden to the principal.

Some examples of pieces of information that may become private knowledge of the agent can be:

- The exact opportunity cost of this task,

- the precise technology used, and how good the matching is between the agent's intrinsic ability and this technology.

In such cases, we will say that there is adverse selection.

文献中，逆向选择可以指"隐藏特征"，也可以指因为隐藏特征而带来的"逆向选择"结果。

3 In order to carry out the delegation of these tasks, the principal and the agent would sign a (bilateral) contract, where the outcomes are verifiable and the consequences are enforceable by a benevolent court of law.

- The key common aspect of all those contracting settings is that the information gap between the principal and the agent has some fundamental implications for the design of the bilateral contract they sign.

  委托人和代理人之间信息的差异在本质上影响了他们所设计的双边合约。

- In order to reach an efficient use of economic resources, this contract must elicit the agent's private information.

为使资源配置达到帕累托有效的程度，合约的设计必须能够揭示出代理人的私有信息。

- This can only be done by giving up some information rent to the privately informed agent, which is costly to the principal.

  这只能通过给予代理人某种租金的方式来实现，而这类租金将成为委托人的成本。

  – This information cost just adds up to the standard technological cost of performing the task and justifies distortions in the volume of trade achieved under asymmetric information.

  这种信息成本加上技术性成本，使得在不对称信息下的交易受到了扭曲。

- The main objective is to characterize the optimal rent extraction-efficiency trade-off faced by the principal when designing his contractual offer to the agent.

  主要目的是刻画委托人所设计的代理合约中最优的租金抽取与配置效率冲突的权衡。

  – The allocative and the informational roles of the contract generally interfere. At the optimal second-best contract, the principal trades off his desire to reach allocative efficiency against the costly information rent given up to the agent to induce information revelation.

  配置功能与信息作用相互冲突。为了诱使代理人说真话所必须付出的信息租金与资源配置效率相互冲突，最后导致了一个次优的合约。

4 We proceed in two steps:

- First, we describe the set of allocations (i.e., output to be produced and a distribution of the gains from trade) that the principal can achieve (despite the information gap),

  首先描述委托人所能达到的资源配置（最终产出和交易收益的分配）集合。

  – incentive compatibility constraints (that are only due to asymmetric information),

  为了诱使代理人如实披露隐藏特征而满足的约束。

  – voluntary participation constraints that ensure that the agent wants to participate in the contract.

  代理人自愿参与交易的约束。

- Second, we proceed by optimizing the principal's objective function within the set of incentive feasible allocations.

  对限制在集合上的委托人目标函数，进行最优化。

5 Consequences of hidden information:

- In general, incentive constraints will be binding at the optimum, showing that adverse selection clearly affects the efficiency of trade.

  在次优解处，激励约束是会起作用的（即绷紧的）。

- As such, the optimal second-best contract calls for

  – a distortion in the volume of trade away from the first-best allocation,

  – and for giving up some strictly positive information rents to the most efficient agents.

6 Implicit assumptions:

- We assume that the principal and the agent both adopt an optimizing behavior and maximize their individual utility.

  – In other words, they are both fully rational individualistic agents.

– Given the contract he receives from the principal, the agent maximizes his utility and chooses output accordingly.

- The principal does not know the agent's private information, but the probability distribution of this information is common knowledge.

  – There exists an objective distribution for the possible types of the agent that is known by both the agent and the principal, and this fact itself is known by the two players.

- The principal is a Bayesian expected utility maximizer.

  – In designing the agent's payoff rule, the principal moves first as a Stackelberg leader under asymmetric information anticipating the agent's subsequent behavior and optimizing accordingly within the set of available contracts.

2   Model

7   Consider a consumer (the principal) who wants to delegate to an agent the production of q units of a good.

8   The value for the principal of these q units is $S(q)$ where $S' > 0$, $S'' < 0$ and $S(0) = 0$.

The marginal value of the good is thus positive and strictly decreasing with the number of units bought by the principal.

9   The production cost of the agent is unobservable to the principal, but it is common knowledge that the marginal cost θ belongs to the set $\Theta = \{\theta_L, \theta_H\}$.

The agent can be either efficient (θ_L) or inefficient (θ_H) with respective probabilities λ and $1 - \lambda$. In other words, he has the cost function

$$c(q, \theta_L) = \theta_L q \text{ with probability } \lambda$$

or

$$c(q, \theta_H) = \theta_H q \text{ with probability } 1 - \lambda.$$

We denote by $\Delta\theta = \theta_H - \theta_L > 0$ the spread of uncertainty on the agent's marginal cost.

Agent has a reservation utility $\bar{u}$, which is assumed to zero. It captures the outside opportunity.

10   The principal's utility, if she purchases q units of the good and pays a monetary transfer t to the agent, is

$$S(q) - t,$$

and at this case the agent's utility is

$$t - c(q, \theta).$$

11   The economic variables are quantity produced q and the transfer t received by the agent.

These variables are both observable and verifiable by a third party such as a benevolent court of law. They can be included in a contract which can be enforced with appropriate penalties if either the principal or the agent deviates from the requested output and transfer.

Let $\mathcal{A}$ be the set of all feasible contract, that is,

$$\mathcal{A} = \{(q, t) \mid q \in \mathbb{R}_+, t \in \mathbb{R}\}.$$

3 Complete information—the first-best outcome

12 First suppose that there is no asymmetry of information between the principal and the agent.

13 The efficient production levels are obtained by maximizing the social value:

$$\max_{q_i \geq 0} S(q_i) - c(q_i, \theta_i) = \max_{q_i \geq 0} S(q_i) - \theta_i q_i.$$

Since $S'' < 0$, the objective function is concave. Then the solution q_i^* must satisfy the first order condition:

$$S'(q_i^*) \begin{cases} \leq \theta_i, \\ = \theta_i, & \text{if } q_i^* > 0. \end{cases}$$

14 The above equation may not have an interior solution.

- Suppose $S'(q_i) > \theta_i$ for any $q_i \geq 0$. Then there is no solution for the maximization problem.
- Suppose $S'(q_i) < \theta_i$ for any $q_i \geq 0$. Then the only solution is the boundary solution: $q_i^* = 0$.

Hereafter, we assume that an interior solution q_i^* exists (and hence it is unique) for both types.

Interpretation: The efficient production levels q_i^* are obtained by equating the principal's marginal value and the agent's marginal cost:

$$S'(q_i^*) = \theta_i.$$

从拥有完全信息的第三方的视角，产量 q_i^* 是社会最优的产量。

15 When the complete-information efficient production levels q_L^* and q_H^* are carried out, the social values W_L^* and W_H^* are respectively

$$W_L^* = S(q_L^*) - \theta_L q_L^* \text{ and } W_H^* = S(q_H^*) - \theta_H q_H^*.$$

Note that the social value W_L^* is always greater than W_H^*:

$$W_L^* = \overbrace{S(q_L^*) - \theta_L q_L^*}^{q_L^* \text{ maximizes } S(q_L) - \theta_L q_L} \geq \underbrace{S(q_H^*) - \theta_L q_H^* \geq S(q_H^*) - \theta_H q_H^*}_{\theta_L < \theta_H} = W_H^*.$$

The complete information efficient production levels q_L^* and q_H^* should be both carried out if their social values are non-negative,

$$W_L^* \geq 0 \text{ and } W_H^* \geq 0.$$

Since W_L^* is always greater than W_H^*, for trade to be always carried out, it is thus enough that production be socially valuable for the least efficient type:

$$W_H^* \geq 0.$$

Since we assume that an interior solution q_i^* exists for both types, this condition automatically holds:

$$W_H^* = S(q_H^*) - \theta_H q_H^* > S(0) - \theta_i \times 0 = 0.$$

3.1 Implementation—payment

16 We have determined the efficient production levels q_i^*.

产量 q_i^* 是第三方视角下的社会最优产量。如果第三方无法强制经济体中的参与者实现这一产量，那么经济体中的参与者是否可以"自发"实现这一社会最优的产量？如果可以，那么如何实现呢？

17 Since the principal cannot force the agent, he must convince the agent to accept the task.

For a successful delegation of the production, the principal must offer the agent a utility level that is at least as high as the utility level that the agent obtains from outside opportunity. We refer to these constraints as the agent's individual rationality constraints or participation constraints.

Here we normalize to zero the agent's outside opportunity utility level (i.e., his status quo utility level), these conditions are written as

$$t_L - \theta_L q_L \geq 0 \text{ and } t_H - \theta_H q_H \geq 0.$$

为了保证"代理人自愿参与交易"的约束。

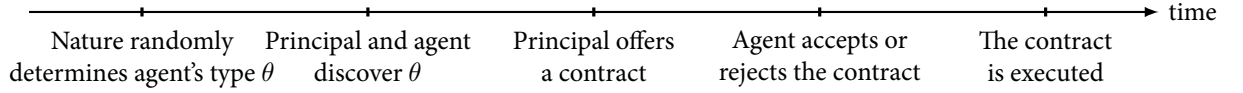18 The sequence of play is as follows:

Figure 1: Timing

19 Obviously, for any θ_i, the contract (q_i^*, t_i^*) satisfies these conditions, if we let $t_i^* = \theta_i q_i^*$.

This contract (q_i^*, t_i^*) is called the first-best contract (or complete-information optimal contract) for θ_i.

20 To implement the first-best production levels q_i^*, the principal can make the following take-it-or-leave-it offers to the agent: If $\theta = \theta_i$, the principal offers the transfer t_i^* for the production level q_i^* with $t_i^* = \theta_i q_i^*$.

Whatever his type, agent accepts the offer and makes zero utility. The complete information optimal contracts are thus (q_L^*, t_L^*) if $\theta = \theta_L$ and (q_H^*, t_H^*) if $\theta = \theta_H$.

如果信息完全，那么可以实现社会最优产量。实现方式是：委托人向代理人 θ_i 提供合约 (q_i^*, t_i^*)（代理人没有议价空间），代理人 θ_i 接受此合约。

此时，委托人给予两类代理人的合约是有差异的——即区别对待或称歧视。

21 Under complete information, delegation is costless for the principal, who achieves the same utility level that he could get if he was carrying out the task himself (with the same cost function as the agent).

这时，社会最优产量实现，即经济体的净收益达到最大。同时，净收益全部归委托人。委托人此时获得了他能够实现的最大收益——相对于最大收益，没有任何损失。

22 Alternative interpretation:

The principal try to maximize her utility subject to inducing the agent to accept the proposed contract. Clearly, the agent obtains 0 if he does not take the principal's contract. So the principal will solve the following problem:

$$\underset{(q_i, t_i) \in \mathcal{A}}{\text{maximize}} \quad S(q_i) - t_i$$

$$\text{subject to} \quad t_i - c(q_i, \theta_i) \geq 0.$$

In any solution, the IR constraint must bind; otherwise, the principal could lower the wage offered and still have the agent accept the contract. Thus, the maximization problem becomes:

$$\max_{q_i \geq 0} S(q_i) - \theta_i q_i.$$

Clearly, $S'' < 0$, and hence the objective function is concave. Then the solution must satisfy the first-order condition:

$$S'(q_i^*) \begin{cases} \leq \theta_i, \\ = \theta_i, & \text{if } q_i^* > 0. \end{cases}$$

Assume there is an interior solution q_i^*, i.e., $S'(q_i^*) = \theta_i$. Then the payment is due to the binding IR constraint: $t_i^* = \theta_i q_i^*$.

3.2 The first-best contract

23 The complete-information optimal contracts are thus (q_L^*, t_L^*) if $\theta = \theta_L$ and (q_H^*, t_H^*) if $\theta = \theta_H$.

24 Every agent (no matter θ_L or θ_H) obtains exactly 0 from principal, just balancing his reservation utility.

25 We denote by V_H^* (resp. V_L^*) the principal's level of utility when he faces the θ_H-(resp. θ_L-) type:

$$V_i^* = S(q_i^*) - \theta_i q_i^* = W_i^*.$$

Interpretation: Because the principal has all the bargaining power in designing the contract, we have $V_i^* = W_i^*$ under complete information.

26 Graphic illustration:

   (a) Agent's reservation utility is 0, which is equivalent to the contract $O = (0, 0)$.

   (b) Principal seeks to find the most profitable point on the isoutility curve with utility 0, i.e., through the point $O = (0, 0)$.

      For the point, the strictly concave indifference curve of the principal is tangent to the zero rent isoutility curve of the corresponding type.

   (c) For a θ_i agent, principal pays t_i^* such that $t_i^* - c(q_i^*, \theta_i) = 0$.

   (d) For a θ_i agent, principal's profit is $V_i^* = S(q_i^*) - c(q_i^*, \theta_i)$.

      This profit is exactly equal to the distance from the origin to the intersection point between the indifference curve through (q_i^*, t_i^*) and the vertical axis:

      i. Principal's indifference curve is of the form $S(q_i) - t = \text{constant}$.

      ii. The constant should be principal's profit, which is V_i^*.

      iii. Letting $q_i = 0$ in the indifference curve $S(q_i) - t_i = V_i^*$, we have $-t_i = V_i^*$. It implies that $V_i^* > 0$.

The complete information optimal contract is finally represented in the following figure by the pair of points (A^*, B^*).
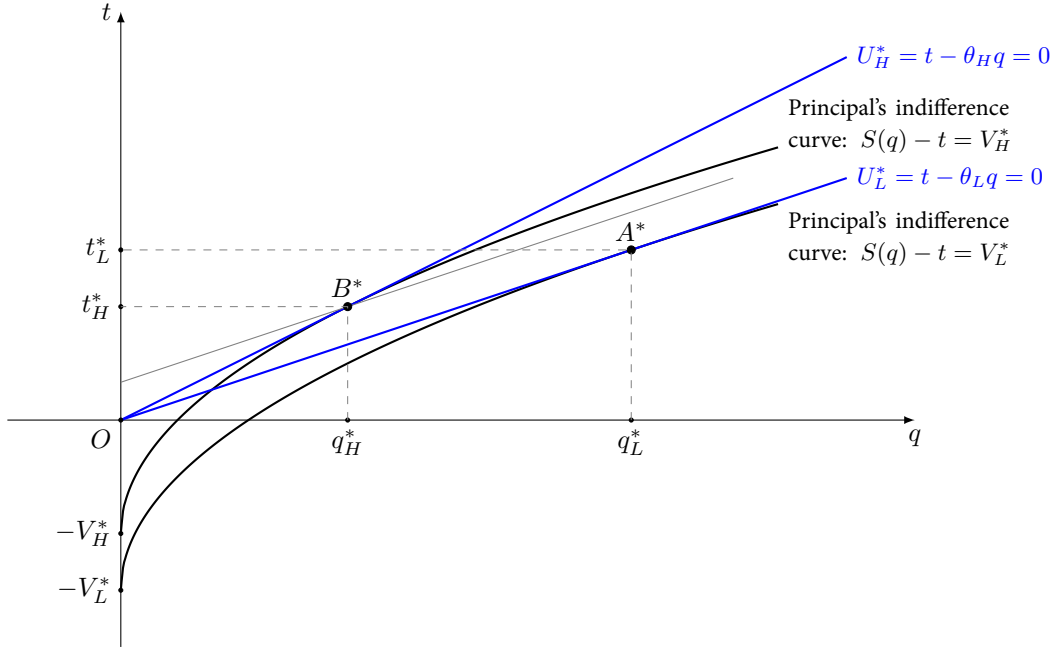
Figure 2: First-best contracts

Suppose instead the reservation utility is $\bar{u} > 0$, which is large enough.

- Then the tangent point and indifference curve will shift up, and hence the profit V_i^* could be negative. In this case, the principal will not provide such a contract—the shutdown occurs.

- Interpretation: If agent's reservation utility is low, principal can attract him to accept some contract; otherwise, agent will not accept any contract that is acceptable for principal.

27 We have $S'(q_i^*) = \theta_i$. Since $S'' < 0$ and $\theta_H > \theta_L$, we have

$$q_L^* > q_H^*,$$

i.e., the optimal production of an efficient agent is greater than that of an inefficient agent.

两类代理人的最优产量的关系明确，高能力代理人的最优产量更高。

28 In the figure, the payment t_L^* is greater than t_H^*, but we note that t_L^* can be greater or smaller than t_H^* depending on the curvature of the function S, as it can be easily seen graphically.

Example: $S(q) = -\frac{4}{q+1} + 4, \theta_L = \frac{1}{4}, \theta_H = 1$. Then $(q_L^*, t_L^*) = (3, \frac{3}{4}), (q_H^*, t_H^*) = (1, 1), V_L^* = \frac{24}{7}, V_H^* = 1$.
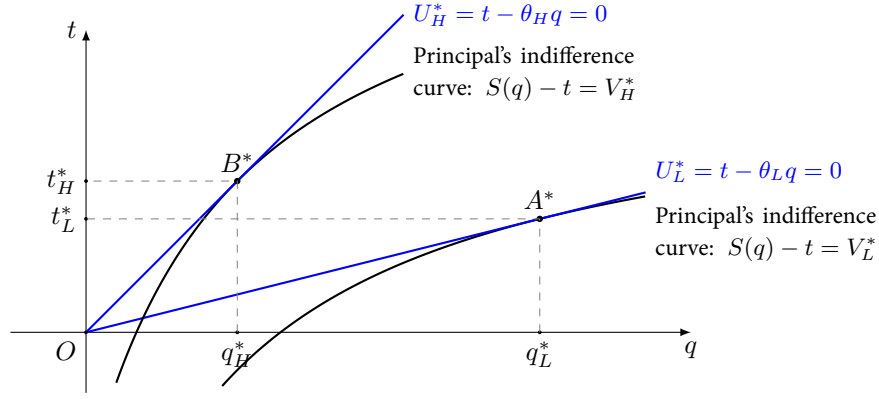
Figure 3: $t_H^* > t_L^*$

两类代理人的最优产量的关系模糊，高能力代理人的工资不一定更高。

29 The principal's utility:

$$V_L^* = W_L^* > W_H^* = V_H^*.$$

From the figure, the indifference curves of the principal correspond to increasing levels of utility when one moves in the southeast direction. Thus, the principal reaches a higher profit when dealing with the efficient type.

4 Incomplete information

30 Suppose that the marginal cost θ is the agent's private information.

We continue to assume that $S'(q_i) = \theta_i$ has a positive solution q_i^*, which implies that $V_i^* = W_i^* > 0$.
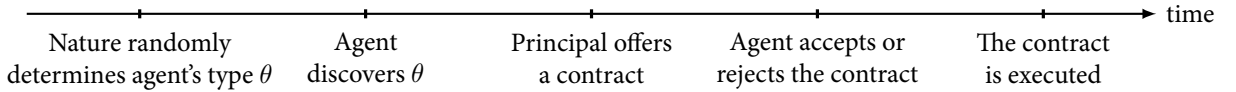
31 The sequence of play is as follows:

Figure 4: Timing

Note that contracts are offered at the interim stage (事中阶段); there is already asymmetric information between the contracting parties when the principal makes his offer.

32 In the following figure, we draw the indifference curves of a θ_L-agent (heavy curves) and of a θ_H-agent (light curves) in the (q, t) space.

The isoutility curves of both types correspond to increasing levels of utility when one moves in the northwest direction. These indifference curves are straight lines with a slope θ corresponding to the agent's type.
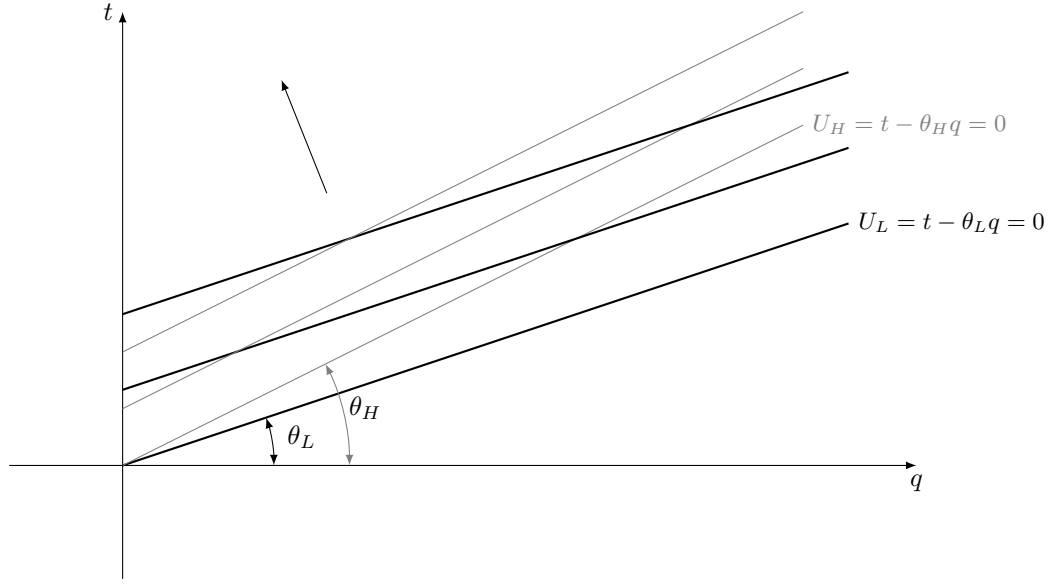
Figure 5: Single-crossing property

Since $\theta_H > \theta_L$, the isoutility curves of the inefficient agent θ_H have a greater slope than those of the efficient agent. Thus, the isoutility curves for different types cross only once. This property is called the single-crossing property (单交叉性质) or Spence-Mirrlees property.

33 Since principal cannot observe agent's type, he cannot offering different contracts for θ_L-agent and θ_H-agent.

In other words, the contract(s) offered to θ_L-agent should coincide with the contract(s) offered to θ_H-agent.

因为委托人无法观察到代理人的类型，所以他无法（像完全信息时）区别对待。

34 In order to reach an efficient use of economic resources, the contract(s) must elicit the agent's private information.

35 Consider the case where the principal offers the menu of contracts $\{(q_L^*, t_L^*), (q_H^*, t_H^*)\}$ hoping that an agent with type θ_L will select (q_L^*, t_L^*) and an agent with type θ_H will select instead (q_H^*, t_H^*).

From Figure 2, we see that B^* is preferred to A^* by both types of agents:

- The θ_L-agent's isoutility curve that passes through B^* corresponds to a positive utility level instead of a zero utility level at A^*.

- The θ_H-agent's isoutility curve that passes through A^* corresponds to a negative utility level, which is less than the zero utility level this type gets by choosing B^*.

Thus, offering the menu (A^*, B^*) fails to have the agents self-selecting properly within this menu. The efficient type mimics the inefficient one and selects also contract B^*. The complete information optimal contracts can no longer be implemented under asymmetric information.

如果直接把完全信息时的两份合约组合在一起，由代理人从中选择，那么两类代理人都将选择合约 (q_H^*, t_H^*)——未能实现"自分离"的结果。

36 A menu of contracts $\{(q_L, t_L), (q_H, t_H)\}$ is incentive compatible (激励相容) when (q_L, t_L) is weakly preferred to (q_H, t_H) by the type-θ_L agent and (q_H, t_H) is weakly preferred to (q_L, t_L) by the type-θ_H agent.

Mathematically,

$$t_L - \theta_L q_L \geq t_H - \theta_L q_H, \tag{IC$_L$}$$

$$t_H - \theta_H q_H \geq t_L - \theta_H q_L. \tag{IC$_H$}$$

37 An IC menu of contracts $\{(q_L, t_L), (q_H, t_H)\}$ is individually rational (个体理性) if

$$t_L - \theta_L q_L \geq 0, \tag{IR$_L$}$$

$$t_H - \theta_H q_H \geq 0. \tag{IR$_H$}$$

We do not require that (q_L, t_L) is acceptable for θ_H agent and (q_H, t_H) is acceptable for θ_L agent, once we assume IC constraints.

38 Example: Pooling contract.

When the contracts targeted for each type coincide and both types of agent accept this contract, we have a pooling contract.

$$q_L = q_H = q^P \text{ and } t_L = t_H = t^P.$$

- Incentive compatibility is trivially satisfied, but at the cost of an obvious loss of flexibility in allocations that are no longer dependent on the state of nature.

- Only the participation constraints matter now; the hardest participation constraint to satisfy is that of the inefficient agent. This is because Equation (IR$_H$) directly implies Equation (IR$_L$) for a pooling contract, which is efficient agent's participation constraint.

Indeed, IC constraints do not rule out the possibility that the contracts designed for agents with different types are the same. Thus, the allocations could be separating or pooling under IC constraints.

39 Example: Shutdown contract.

When one of the contracts is the null contract $(0,0)$ and the nonzero contract (q^s, t^s) is only accepted by the efficient type.

- Then, Equation (IC$_L$) and Equation (IR$_L$) both reduce to $t^s - \theta_L q^s \geq 0$.

- The Equation (IC$_H$) reduces to $0 \geq t^s - \theta_H q^s$. If this inequality is strict, only the efficient type accepts the contract.

- With such a contract, the principal gives up production if the agent is a θ_H-type. We will say that it is a contract with shutdown of the least efficient type.

In particular, $\{(q_L^*, t_L^*), (0,0)\}$ is a shutdown contract, where the contract (q_L^*, t_L^*) is only accepted by the efficient type.

40 If a menu of contracts $\{(q_L, t_L), (q_H, t_H)\}$ is incentive compatible, then

$$\overbrace{\theta_L(q_H - q_L) \geq}^{\text{By Equation (IC$_L$)}} \underbrace{t_H - t_L \geq \theta_H(q_H - q_L)}_{\text{By Equation (IC$_H$)}},$$

and hence

$$q_H - q_L \leq 0. \tag{M}$$

It is called the monotonicity constraint.

Incentive compatibility alone (regardless of the principal's preferences) implies that the production level requested from a θ_H-agent cannot be higher than the one requested from a θ_L-agent.

41 A pair of outputs (q_L, q_H) is said to be implementable if it can be reached by an incentive compatible contract.

Implementability is equivalent to monotonicity constraint. Suppose $q_H - q_L \leq 0$. For IC constraints to satisfy, we should have

$$t_L - \theta_L q_L \geq t_H - \theta_L q_H \text{ and } t_H - \theta_H q_H \geq t_L - \theta_H q_L.$$

Then we have

$$\theta_L(q_H - q_L) \geq t_H - t_L \geq \theta_H(q_H - q_L).$$

It is enough to take transfers (t_L, t_H) such that the above equation holds.

4.1 Principal's problem

42 Recall that under complete information, the principal is able to maintain all types of agents at their zero status quo utility level. Their respective utility levels U_L^* and U_H^* at the first-best contracts satisfy

$$U_L^* = t_L^* - \theta_L q_L^* = 0 \text{ and } U_H^* = t_H^* - \theta_H q_H^* = 0.$$

Generally this will not be possible anymore under incomplete information, at least when the principal wants both types of agents to be active.

43 Take any IC and IR menu of contracts $\{(q_L, t_L), (q_H, t_H)\}$. Let

$$U_L = t_L - \theta_L q_L \geq 0 \text{ and } U_H = t_H - \theta_H q_H \geq 0$$

denote the respective information rent (the utility in excess of the reservation utility) of each type.

信息租金：信息不对称导致的委托人收益的下降（或代理人收益的增加）。

(a) Consider the utility level that a θ_L-agent would get by mimicking a θ_H-agent. By doing so, he would get

$$t_H - \theta_L q_H = t_H - \theta_H q_H + \theta_H q_H - \theta_L q_H = U_H + \Delta\theta q_H.$$

(b) IC constraint guarantees that $U_L = t_L - \theta_L q_L \geq t_H - \theta_L q_H = U_H + \Delta\theta q_H$.

(c) As such, even if the θ_H-agent utility level is reduced to its lowest utility level fixed at zero; that is, $U_H = t_H - \theta_H q_H = 0$, the θ_L-agent benefits from an information rent $\Delta\theta q_H$ coming from his ability to possibly mimic the less efficient type.

(d) So, as long as the principal insists on a positive output for the inefficient type (i.e., $q_H > 0$), the principal must give up a positive rent to a θ_L-agent. This information rent is generated by the informational advantage of the agent over the principal.

为了避免 θ_L 代理人模仿 θ_H 代理人，需要保证 θ_L 代理人的收益 U_L 不低于 $U_H + \Delta\theta q_H$。后者很可能是个正数，这使得 θ_L 代理人获得了一个正的收益。因为在完全信息下收益是零，因此这个正收益就是信息租金。

(How about θ_H-agent mimicking θ_L-agent?)

The principal's problem is to determine the smartest way to give up the rent provided by any given IC and IR menu of contracts.

44 According to our timing of the contractual game, the principal must offer a menu of contracts before knowing which type of agent he is facing.

Therefore, he will compute the benefit of any menu of contracts $\{(q_L, t_L), (q_H, t_H)\}$ in expected terms.

The principal's problem is to solve

$$\underset{(q_L, t_L),(q_H, t_H)}{\text{maximize}} \quad \lambda\big(S(q_L) - t_L\big) + (1 - \lambda)\big(S(q_H) - t_H\big)$$

$$\text{subject to} \quad \text{Constraints (IC}_L)\text{–(IR}_H).$$

45 Since $U_L = t_L - \theta_L q_L$ and $U_H = t_H - \theta_H q_H$, we can replace transfers in the principal's objective function as functions of information rents and outputs so that the new optimization variables are now $\{(q_L, U_L), (q_H, U_H)\}$. The focus on outputs allows us to analyze its impact on allocative efficiency and the overall gains from trade.

46 With this change of variables, the principal's objective function can then be rewritten as

$$\underbrace{\lambda\big(S(q_L) - \theta_L q_L\big) + (1 - \lambda)\big(S(q_H) - \theta_H q_H\big)}_{\text{Expected social value/allocative efficiency}} - \underbrace{\big(\lambda U_L + (1 - \lambda)U_H\big)}_{\text{Expected information rent}}.$$

This new expression clearly shows that the principal wishes to maximize the expected social value of trade minus the expected rent of the agent.

There is a tradeoff between distortions away from efficiency in order to decrease the agent's information rent.

47 The incentive constraints and individual rationality constraints are rewritten as

$$U_L \geq U_H + \Delta\theta q_H, \tag{IC$_L'$}$$

$$U_H \geq U_L - \Delta\theta q_L, \tag{IC$_H'$}$$

$$U_L \geq 0, \tag{IR$_L'$}$$

$$U_H \geq 0. \tag{IR$_H'$}$$

4.2 Solving the principal's problem

48 The major technical difficulty of principal's problem, and more generally of incentive theory, is to determine which of the many constraints imposed by incentive compatibility and participation are the relevant ones, i.e., the binding ones at the optimum of the principal's problem.

49 Step 1: The constraint (IR$_L'$) is always satisfied due to constraints (IC$_L'$) and (IR$_H'$).

The ability of the θ_L-agent to mimic the θ_H-agent implies that the θ_L-agent's participation constraint is always satisfied.

If a menu of contracts enables a θ_H-agent to reach his status quo utility level, it will also be the case for a θ_L-agent who can produce at a lower cost.
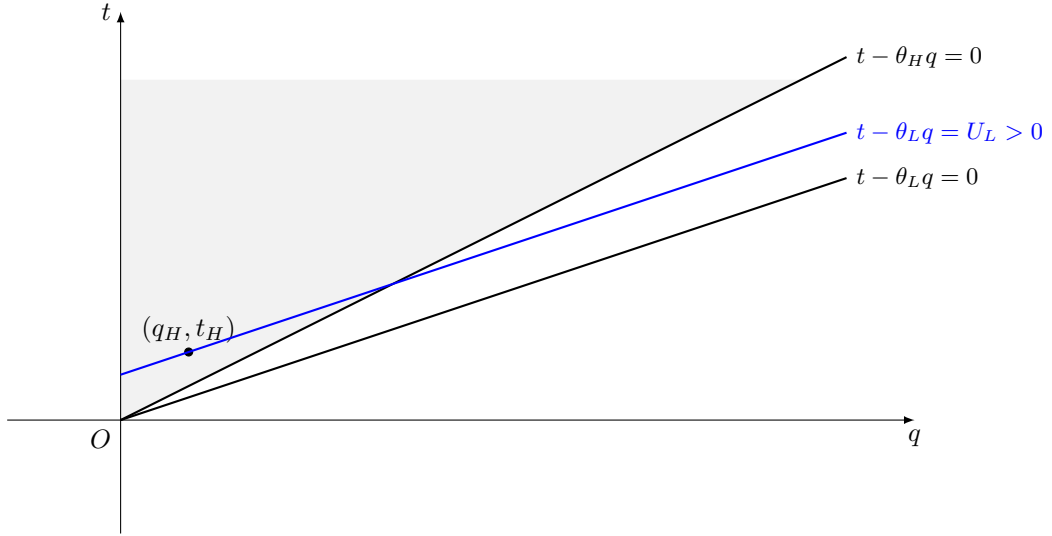
Figure 6: IR for θ_L

Graphic illustration:

(a) By Equation (IR$'_H$), (q_H, t_H) must lie in the shaded region.

(b) By Equation (IC$'_L$), (q_L, t_L) must lie on or above the θ_L-indifference curve through (q_H, t_H).

(c) This implies that θ_L-agent's utility is at least 0.

50 Step 2: The constraint (IR$'_H$) is binding at the optimum, i.e., $U_H = 0$.

Suppose that $U_H = \varepsilon > 0$ at the optimum. Then the principal can decease U_H by ε and consequently also U_L by ε and gain ε. Contradiction.

51 Step 3: The constraint (IC$'_L$) is binding at the optimum, i.e., $U_L = \Delta\theta q_H$.

Suppose that $U_L - \Delta\theta q_H = \varepsilon > 0$ at the optimum. Then the principal can decrease U_L by ε and gain $\lambda\varepsilon$. Contradiction.

52 IC for θ_H-agent seems irrelevant because the difficulty comes from a θ_L-agent willing to claim that he is inefficient rather than the reverse.

We ignore this condition for now and then get a solution. We will verify whether the solution satisfies this condition.

When (IC$'_L$) is binding, (IC$'_H$) is equivalent to (M):

$$t_H - \theta_H q_H - t_L + \theta_H q_L = \Delta\theta(q_L - q_H).$$

Thus, it suffices to verify (M) later.

53 Step 4: By Steps 2 and 3, we obtain a reduced program

$$\underset{q_L, q_H}{\text{maximize}} \quad \lambda\big(S(q_L) - \theta_L q_L\big) + (1 - \lambda)\big(S(q_H) - \theta_H q_H\big) - \lambda\Delta\theta q_H.$$

Compared with the full information setting, asymmetric information alters the principal's optimization simply by the subtraction of the expected rent that has to be given up to the efficient type.

13

The inefficient type gets no rent, but the efficient type θ_L gets the information rent that he could obtain by mimicking the inefficient type θ_H. This rent depends only on the level of production requested from this inefficient type.

54 Step 5: The first order condition on q_L implies

$$S'(q_L^{\text{SB}}) = \theta_L, \text{ that is, } q_L^{\text{SB}} = q_L^*.$$

Hence, there is no distortion away from the first-best for the efficient type's output. Here, the superscript SB means the second-best.

高能力代理人的次优产量与最优产量相等，没有扭曲。

55 Step 6: The first order condition on q_H implies

$$(1 - \lambda)\big(S'(q_H^{\text{SB}}) - \theta_H\big) \begin{cases} \leq \lambda\Delta\theta, \\ = \lambda\Delta\theta, & \text{if } q_H^{\text{SB}} > 0. \end{cases}$$

Since we have assumed $S'(q_H^*) - \theta_H = 0$, the equation above does have a solution. When q_H decreases from q_H^*, LHS increases from 0. On one hand, if LHS reaches $\lambda\Delta\theta$ at $q_H^{\text{SB}} > 0$, then this q_H^{SB} is the optimal solution. On the other hand, if LHS is always lower than $\lambda\Delta\theta$ for any $q_H > 0$, then the solution is $q_H^{\text{SB}} = 0$.

We first assume there is an interior solution q_H^{SB}. That is,

$$(1 - \lambda)\big(S'(q_H^{\text{SB}}) - \theta_H\big) = \lambda\Delta\theta.$$

This equation expresses the important trade-off between efficiency and rent extraction which arises under asymmetric information.

- LHS is the expected marginal efficiency gain (resp. cost) by an infinitesimal increase (resp. decrease) of the inefficient type's output are equated.

  期望效率的边际。

- RHS is the expected marginal cost (resp. gain) of the rent brought about by an infinitesimal increase (resp. decrease) of the inefficient type's output are equated.

  期望信息租金的边际。

At the second-best optimum, the principal is neither willing to increase nor to decrease the inefficient agent's output.

56 Step 7: We have the following inequality

$$q_L^{\text{SB}} = q_L^* > \underbrace{q_H^* > q_H^{\text{SB}}}_{S'' < 0},$$

and hence

$$U_H^{\text{SB}} = 0 > \Delta\theta q_H^{\text{SB}} - \Delta\theta q_L^{\text{SB}} = U_L^{\text{SB}} - \Delta\theta q_L^{\text{SB}}.$$

That is, the constraints (M) and (IC$_H'$) are satisfied.

向上的激励相容条件（upward incentive compatibility，低能力模仿高能力）不是问题。另一方面，向下的激励相容条件（downward incentive compatibility，高能力模仿低能力）更为关键，需要谨慎处理。

57 We have assumed that the equation $(1 - \lambda)\big(S'(q_H) - \theta_H\big) = \lambda\Delta\theta$ admits an interior solution (which is unique).

Theorem (Optimal contract without shutdown): Under asymmetric information, the optimal menu of contracts entails:

- No output distortion for the efficient type with respect to the first-best, $q_L^{\text{SB}} = q_L^*$.

- A downward output distortion for the inefficient type, $q_H^{\text{SB}} < q_H^*$ with

$$S'(q_H^{\text{SB}}) = \theta_H + \frac{\lambda}{1-\lambda}\Delta\theta.$$

Here we have assumed that the equation above has positive solution. Otherwise q_H^{SB} should be set at zero, and we are in the special case of a contract with shutdown, which will be discussed later.

Note that

$$q_L^{\text{SB}} = q_L^* > q_H^* > q_H^{\text{SB}}.$$

- Only the efficient type gets a positive information rent given by

$$U_L^{\text{SB}} = \Delta\theta q_H^{\text{SB}}.$$

- The second-best transfers are respectively given by

$$t_L^{\text{SB}} = \theta_L q_L^* + \Delta\theta q_H^{\text{SB}} > \theta_L q_L^* = t_L^* \text{ and } t_H^{\text{SB}} = \theta_H q_H^{\text{SB}} < \theta_H q_H^* = t_H^*.$$

Note that
$$t_L^{\text{SB}} = \theta_L q_L^* + \Delta\theta q_H^{\text{SB}} = \theta_L q_L^* + \theta_H q_H^{\text{SB}} - \theta_L q_H^{\text{SB}} = t_H^{\text{SB}} + \theta_L(q_L^* - q_H^{\text{SB}}) > t_H^{\text{SB}}.$$

58 "顶部无扭曲"与"单向扭曲/向下扭曲"是两条最基本的规律。

- 对于高能力，不存在产出水平的扭曲（其产出水平与完全信息最优时的产出水平一致），但代价是需要给其支付信息租金。

- 对于低能力，其付出的产出水平低于完全信息最优时的产出水平，但没有信息租金。

4.3 Graphic illustration

59 $q_H^{\text{SB}} \leq q_H^*$.

   (a) Suppose $q_H^{\text{SB}} > q_H^*$.

   (b) Since θ_H-IR binds, $(q_H^{\text{SB}}, t_H^{\text{SB}})$ lies on the indifference curve through $(0,0)$.

   (c) To make θ_H-IC and θ_L-IC hold, $(q_L^{\text{SB}}, t_L^{\text{SB}})$ lies in the shaded region.

   (d) Principal can raise her profit by moving $(q_H^{\text{SB}}, t_H^{\text{SB}})$ to (q_H^*, t_H^*): θ_H-IC and θ_L-IC still hold.

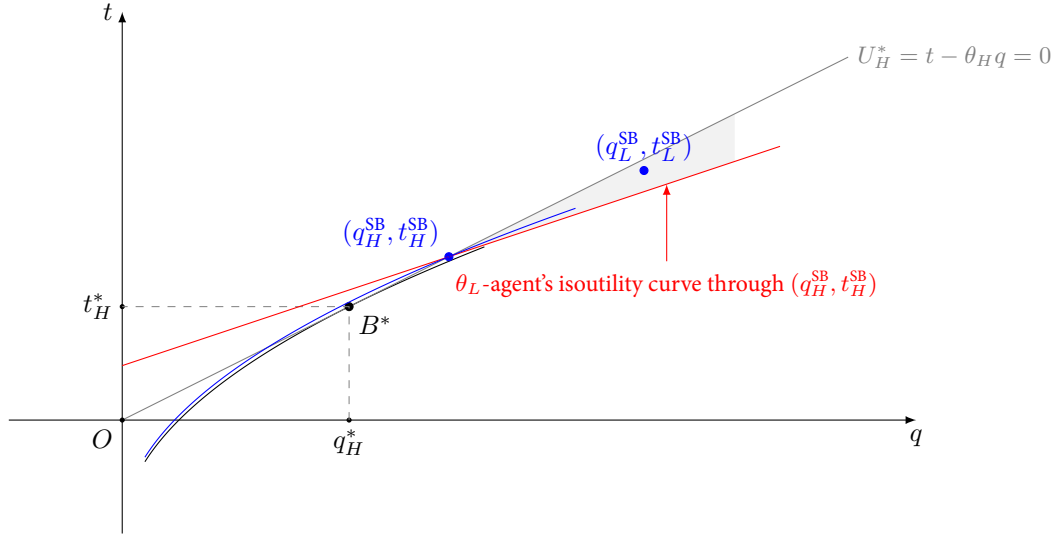   (e) Thus, $q_H^{\text{SB}} > q_H^*$ cannot be optimal.

Figure 7: $q_H^{SB} \leq q_H^*$

60 $q_L^{SB} = q_L^*$.

(a) Suppose that $q_H^{SB} \leq q_H^*$.

(b) To make θ_H-IC and θ_L-IC hold, (q_L^{SB}, t_L^{SB}) lies in the shade region.

(c) Principal's problem is to find the allocation of (q_L^{SB}, t_L^{SB}) that maximizes her profit.

(d) The optimal solution occurs at a point of tangency between the indifference curve of θ_L-agent through (q_L^{SB}, t_L^{SB}) and an isoprofit curve for principal.

(e) All points of tangency between indifference curves of θ_L-agent and isoprofit curves of principal occur at q_L^*.
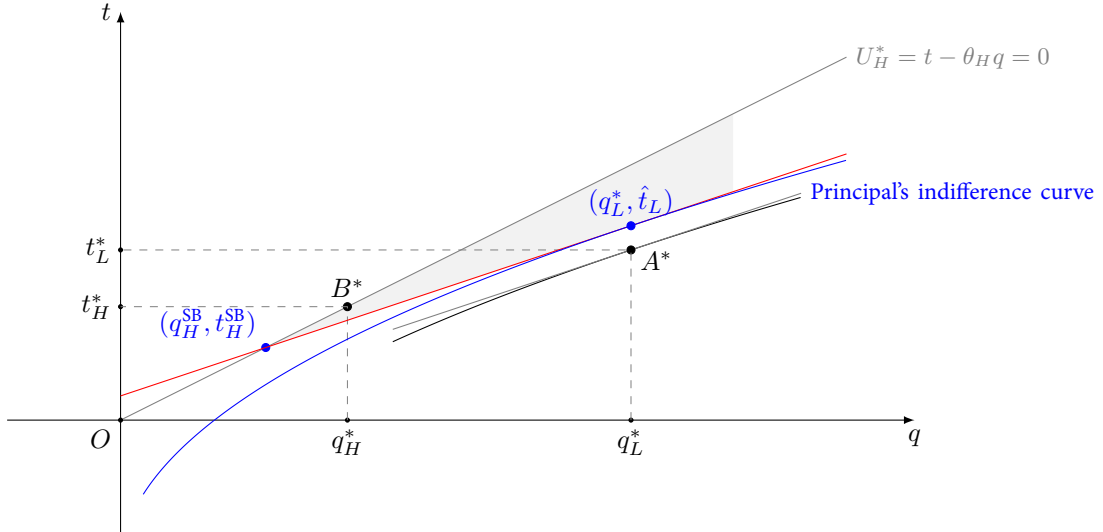

Figure 8: $q_L^{SB} = q_L^*$

61 Starting from the complete information optimal contract (A^*, B^*) that is not incentive compatible, we can construct an incentive compatible contract (C, B^*) with the same production levels by giving a higher transfer to the agent producing q_L^* (Figure 9).
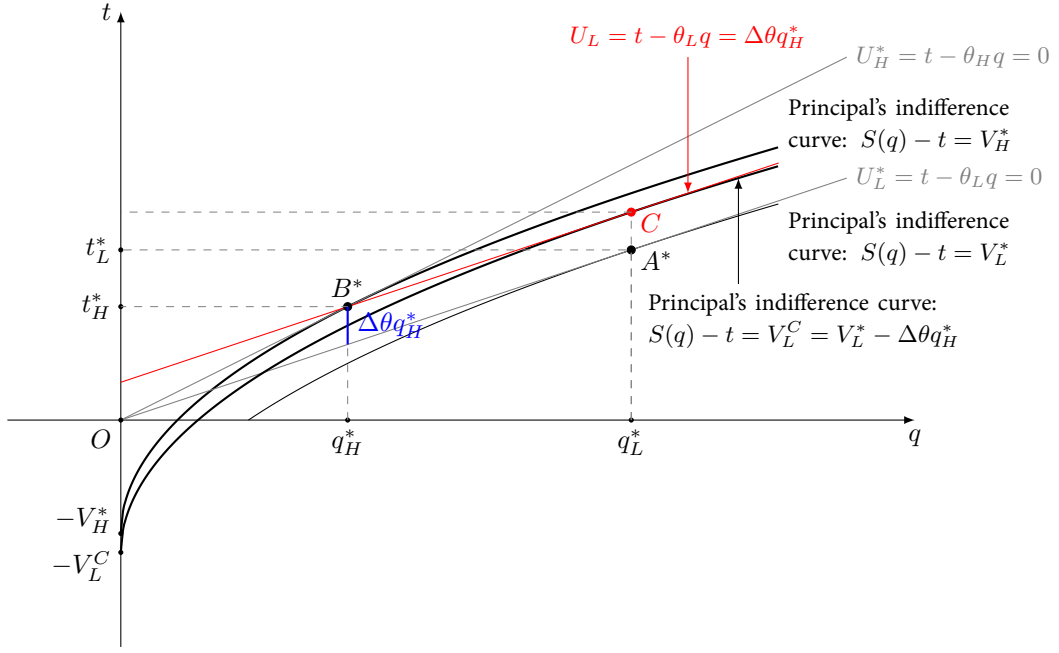
Figure 9: Rent needed to implement the first-best outputs

(a) The contract C is on the θ_L-agent's indifference curve passing through B^*.

(b) Hence, the θ_L-agent is now indifferent between B^* and C. (B^*, C) becomes an incentive-compatible menu of contracts.

(c) The rent that is given up to the θ_L-agent is now $\Delta\theta q_H^*$.

62 Rather than insisting on the first-best production level q_H^* for an inefficient type, the principal can slightly decrease q_H by a small amount.
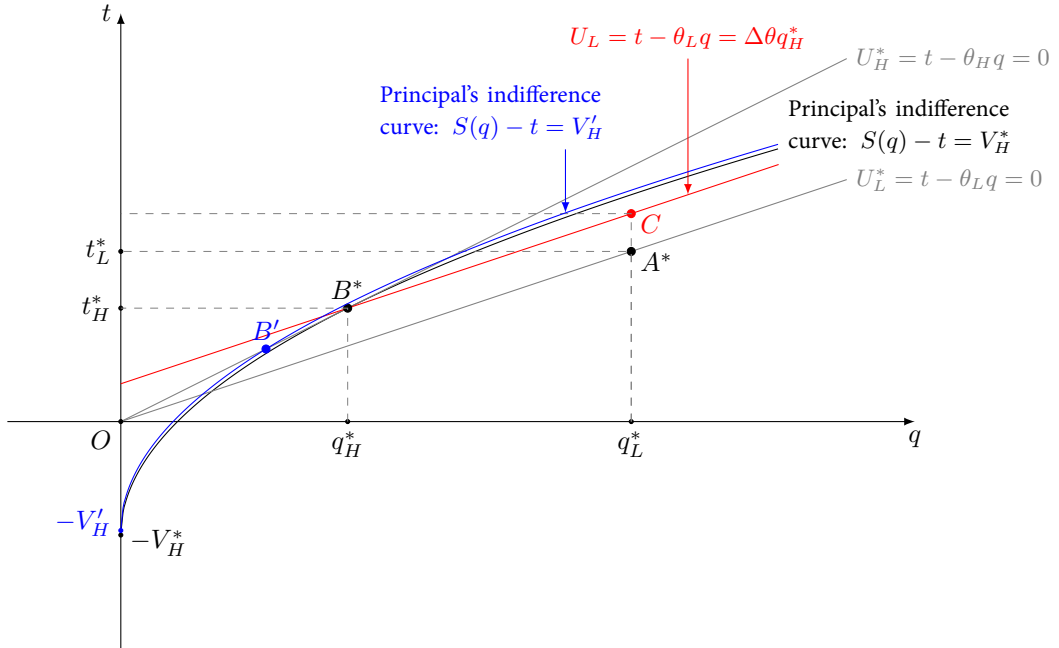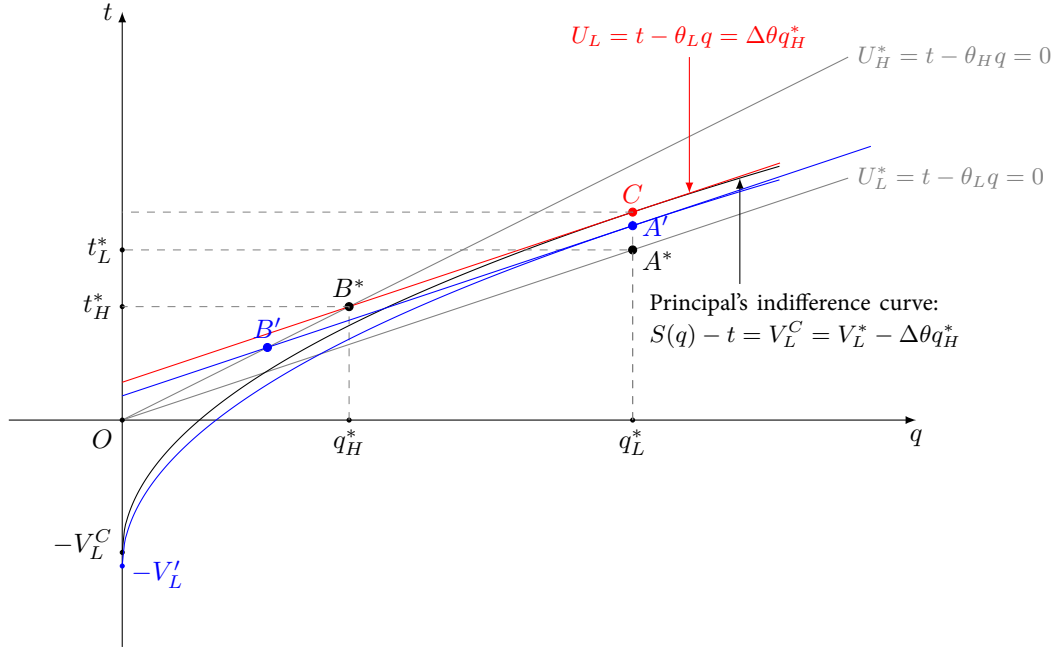

Figure 10: Profit loss in θ_H

Figure 11: Profit gain in θ_L

(a) Principal firstly moves $B^* = (q_H^*, t_H^*)$ downwards along θ_H-agent's indifference curve through $(0,0)$, for example, to B'.

(b) This change lowers the profit that principal earns from θ_H agents: from V_H^* to $V_H' < V_H^*$. (Figure 10)

(c) On the other hand, it relaxes θ_L-agent's IC constraint.

(d) Principal then moves C to A'.

(e) This change increases the profit that principal earns from θ_L agents: from V_L^C to $V_L' > V_L^C$. (Figure 11)

(f) Comparison: By slightly decreasing q_H (from q_H^*) by an amount $\mathrm{d}q$:

- By doing so, expected efficiency is just diminished by a second-order term $\frac{1}{2}|S''(q_H^*)|(\mathrm{d}q)^2$ since q_H^* is the first-best output that maximizes efficiency when the agent is inefficient:

$$\left[S(q_H^* - \mathrm{d}q) - \theta_H(q_H^* - \mathrm{d}q)\right] - \left[S(q_H^*) - \theta_H q_H^*\right] = \frac{1}{2}S''(q_H^*)(\mathrm{d}q)^2 + o\big((\mathrm{d}q)^3\big).$$

- Instead, the information rent left to the efficient type diminishes to the first-order term $\Delta\theta\,\mathrm{d}q$:

$$\left[\Delta\theta(q_H^* - \mathrm{d}q)\right] - \Delta\theta q_H^* = -\Delta\theta\,\mathrm{d}q.$$

- Thus, it is profitable for principal to slightly reduce q_H.

- Alternatively, the marginal return from reducing q_H is higher than the marginal cost from reducing q_H:

$$\lambda\Delta\theta > 0 = (1 - \lambda)\left(S'(q_H^*) - \theta_H\right).$$

(g) Of course, the principal stops reducing the inefficient type's output when a further decrease would have a greater efficiency cost than the gain in reducing the information rent it would bring about:

$$\lambda\Delta\theta = (1 - \lambda)\left(S'(q_H^{\text{SB}}) - \theta_H\right).$$

The optimal trade-off finally occurs at $(A^{\text{SB}}, B^{\text{SB}})$ as shown in Figure 12.

(h) There is the other case: it would be possible that

$$\lambda\Delta\theta > (1-\lambda)\left(S'(q_H) - \theta_H\right)$$

holds for any $q_H > 0$. In other words, the marginal return is always higher than the marginal cost. Thus, q_H will decrease to the lower bound 0. That is the case with shutdown.
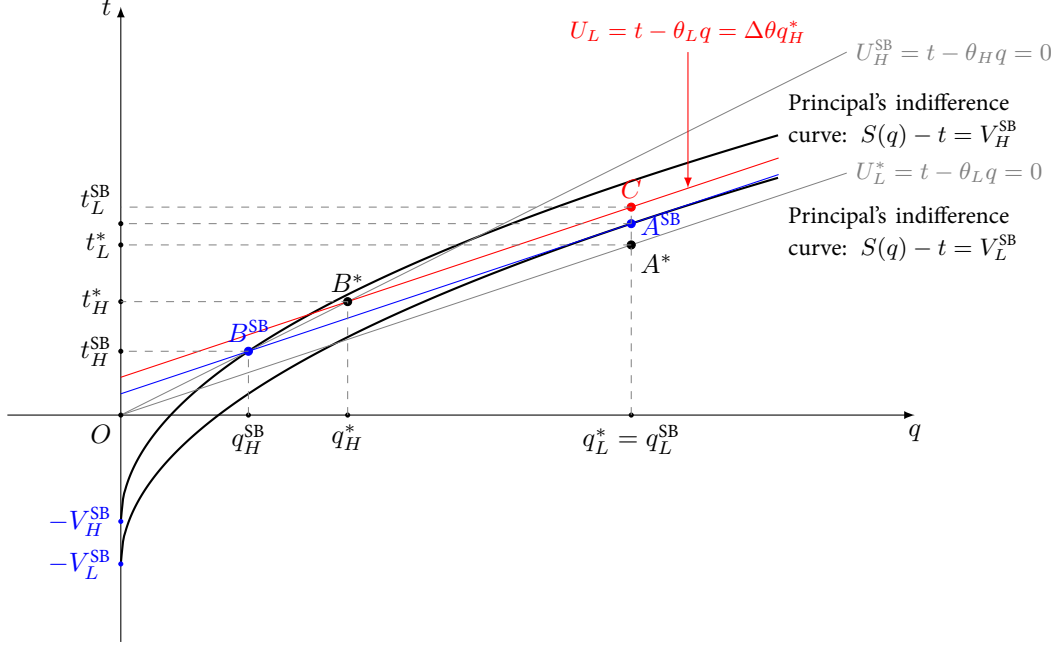

Figure 12: Second-best contracts

63 配置效率与信息租金之间的权衡：

- 为了让 θ_L 代理人选择为其设计的产出水平，需要给他一定好处的信息租金；该信息租金取决于 θ_H 代理人的产出水平，以及 θ_L 和 θ_H。
- 之所以降低 θ_H 代理人的产出水平，是为了尽可能减少支付给 θ_L 代理人的信息租金。
- 委托人扭曲的 θ_H 代理人的产出水平，依赖于两种代理人之间的差异。
  - 当 $\theta_H - \theta_L \to 0$ 时，θ_L 代理人的信息租金趋于零，此时 θ_H 代理人会趋于有效的产出水平 q_H^*。
  - 而当 $\theta_H - \theta_L \to \infty$ 时，θ_L 代理人的信息租金趋于无穷大，此时委托人会采取将 θ_H 代理人停工的排斥性合约，以避免支付高额的信息租金。

4.4   Optimal contract with shutdown

64 Consider the first order condition of θ_H-agent:

$$(1-\lambda)\left(S'(q_H^{\text{SB}}) - \theta_H\right) \begin{cases} \leq \lambda\Delta\theta, \\ = \lambda\Delta\theta, & \text{if } q_H^{\text{SB}} > 0. \end{cases}$$

We assumed $S'(q_H^{\text{SB}}) = \theta_H + \frac{\lambda}{1-\lambda}\Delta\theta$ has a positive solution.

65 Consider the case that the first order condition has a boundary solution.

Theorem (Optimal contract with shutdown).

(a) If the equation $S'(q_H^{\text{SB}}) = \theta_H + \frac{\lambda}{1-\lambda}\Delta\theta$ has no positive solution, then the solution q_H^{SB} should be zero.

(b) Then B^{SB} coincides with O and A^{SB} with A^* in Figure 12.

(c) No rent is given up to the θ_L-agent by the unique non-null contract (q_L^*, t_L^*) offered and selected only by agent θ_L.

(d) The shutdown of the agent occurs when $\theta = \theta_L$.

With such a contract, a significant inefficiency emerges because the inefficient type does not produce. The benefit of such a contract is that no rent is given up to the efficient type.

因为一阶条件有解（可以是内点解，也可以是边界解），因此可以先假定解是内点形式，然后利用"等号成立的一阶条件"进行求解。如果得到的解是内点的，那么万事大吉，它就是一阶条件的（内点）解。如果得到的解不是内点的（甚至没有解），那么一阶条件就没有内点解，它的解就是边界解。简言之，直接求解"等号成立的一阶条件"，若得到内点解，那么它就是一阶条件的解，否则一阶条件的解是边界解。

66 直觉：

- 如果 θ_L 代理人的比例很大（λ 接近于 1），导致一阶条件没有正数解：若给 θ_H 代理人提供非零合约，或者说提高 θ_H 代理人的配置效率，则甄别中需要支付给 θ_L 代理人过多的信息租金，对于委托人并不划算。

- 如果两种代理人的差异较大（$\theta_H - \theta_L$ 很大），导致一阶条件没有正数解：若给 θ_H 代理人提供非零合约，则甄别中需要支付给 θ_L 代理人过多的信息租金，委托人也会选择不给 θ_H 代理人提供合约。

67 Numerical example: $S(q) = \log(q+1), \theta_H = \frac{1}{2}, \theta_L = \frac{1}{3}, \lambda = \frac{6}{7}$.

The first order condition is

$$\tfrac{1}{7}\big(\tfrac{1}{q_H^{\text{SB}}+1} - \theta_H\big) \begin{cases} \leq \frac{6}{7}\Delta\theta, \\ = \frac{6}{7}\Delta\theta, & \text{if } q_H^{\text{SB}} > 0. \end{cases}$$

Consider the equation

$$\tfrac{1}{7}\big(\tfrac{1}{q_H+1} - \theta_H\big) = \tfrac{6}{7}\Delta\theta.$$

We get the solution $q = -\frac{1}{3} < 0$. Thus, the solution should be $q_H^{\text{SB}} = 0$.

68 More generally, such a shutdown contract is optimal when

$$\lambda\big(S(q_L^*) - \theta_L q_L^*\big) \geq \lambda\big(S(q_L^{\text{SB}}) - \theta_L q_L^{\text{SB}} - \Delta\theta q_H^{\text{SB}}\big) + (1-\lambda)\big(S(q_H^{\text{SB}}) - \theta_H q_H^{\text{SB}}\big)$$

or, noting that $q_L^* = q_L^{\text{SB}}$, when

$$\lambda\Delta\theta q_H^{\text{SB}} \geq (1-\lambda)\big(S(q_H^{\text{SB}}) - \theta_H q_H^{\text{SB}}\big).$$

- The left-hand side represents the expected cost of the efficient type's rent due to the presence of the inefficient one when the latter produces a positive amount q_H^{SB}.

- The right-hand side represents the expected benefit from transacting with the inefficient type at the second-best level of output.

- Thus, shutdown for the inefficient type is optimal when this expected benefit is lower than the expected cost.

69 When Inada condition $S'(0) = +\infty$ is satisfied and $\lim_{q\to 0} S'(q)q = 0$, the shutdown is never desirable.

(1) q_H^{SB} defined by $S'(q_H^{\text{SB}}) = \theta_H + \frac{\lambda}{1-\lambda}\Delta\theta$ is necessarily strictly positive since $S'(0) = +\infty$.

(2)

$$S(q_H^{\text{SB}}) - \left(\theta_H + \frac{\lambda}{1-\lambda}\Delta\theta\right)q_H^{\text{SB}} = S(q_H^{\text{SB}}) - S'(q_H^{\text{SB}})q_H^{\text{SB}}$$

is strictly positive since $S(q) - S'(q)q$ is strictly increasing with q and is equal to zero for $q = 0$. Hence,

$$\lambda\Delta\theta q_H^{\text{SB}} < (1-\lambda)\left(S(q_H^{\text{SB}}) - \theta_H q_H^{\text{SB}}\right)$$

and the shutdown of the least efficient type does not occur.

5 General utility function for the agent

70 Consider a general cost function $C(q, \theta)$ with the assumption

$$C(0, \theta) = 0, \ C_q > 0, \ C_\theta > 0, \ C_{qq} > 0, \ C_{qq\theta} > 0.$$

71 The generalization of the Spence-Mirrlees property used so far is now

$$C_{q\theta} > 0.$$

This condition still ensures that the different types of the agent have indifference curves which cross each other at most once.

(a) A typical indifference curve of θ-agent is $t - C(q, \theta) = $ constant, i.e., $t = C(q, \theta) + $ constant. Then, at any (q, t), the marginal rate of substitution between transfers and outputs is

$$\frac{\mathrm{d}t}{\mathrm{d}q} = C_q(q, \theta),$$

which describes the slope of the indifference curve.

(b) The slope $C_q(q, \theta)$ is increasing in θ since $C_{q\theta}(q, \theta) > 0$. Thus, at a given point $(\hat{q}, \hat{t})$, for two indifference curves passing it,

$$\text{Slope of } \theta_L\text{-indifference curve} = \left.\frac{\mathrm{d}t(q, \theta_L)}{\mathrm{d}q}\right|_{(\hat{q}, \hat{t})} = C_q(\hat{q}, \theta_L)$$

$$< C_q(\hat{q}, \theta_H) = \left.\frac{\mathrm{d}t(q, \theta_H)}{\mathrm{d}q}\right|_{(\hat{q}, \hat{t})} = \text{Slope of } \theta_H\text{-indifference curve}.$$

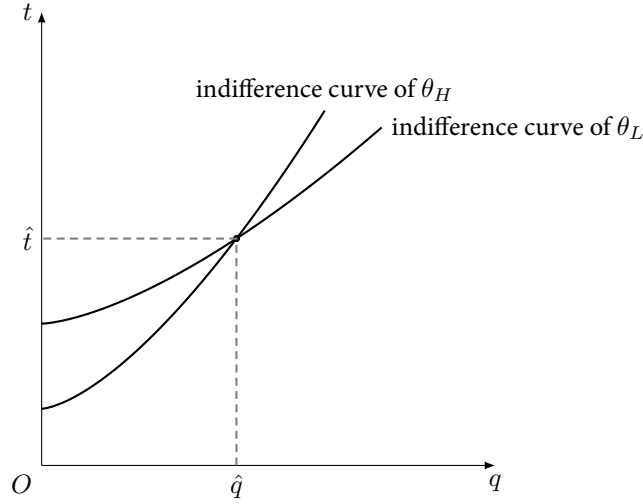(c) The increasing rate of slope $C_{qq}(q, \theta)$ is increasing in θ since $C_{qq\theta} > 0$.

Figure 13: Spence-Mirrlees property

72 It is obviously satisfied in the linear case $C(q,\theta) = \theta q$ that was analyzed before.

Economically, this Spence-Mirrlees property is quite clear; it simply says that a more efficient type is also more efficient at the margin.

73 Incentive compatibility constraints are

$$t_L - C(q_L, \theta_L) \geq t_H - C(q_H, \theta_L),$$
$$t_H - C(q_H, \theta_H) \geq t_L - C(q_L, \theta_H).$$

Individual rationality constraints are

$$t_L - C(q_L, \theta_L) \geq 0 \text{ and } t_H - C(q_H, \theta_H) \geq 0.$$

74 IC constraints imply monotonicity constraint:

$$\int_{q_H}^{q_L} C_q(q, \theta_H)\, \mathrm{d}q = \overbrace{C(q_L, \theta_H) - C(q_H, \theta_H) \geq \underbrace{t_L - t_H}_{\text{By } \theta_L\text{-IC}} \geq C(q_L, \theta_L) - C(q_H, \theta_L)}^{\text{By } \theta_H\text{-IC}} = \int_{q_H}^{q_L} C_q(q, \theta_L)\, \mathrm{d}e,$$

and hence $q_L \geq q_H$.

75 Let $U_L = t_L - C(q_L, \theta_L)$ and $U_H = t_H - C(q_H, \theta_H)$ denote information rents. Then we can rewrite the constraints as:

$$U_L \geq U_H + \Phi(q_H),$$
$$U_H \geq U_L - \Phi(q_L),$$
$$U_L \geq 0,$$
$$U_H \geq 0,$$

where $\Phi(q) = C(q, \theta_H) - C(q, \theta_L)$. Then $\Phi'(q) = C_q(q, \theta_H) - C_q(q, \theta_L) > 0$ and $\Phi''(q) = C_{qq}(q, \theta_H) - C_{qq}(q, \theta_L) > 0$.

22

76 Following the same steps as before, the incentive constraint of an efficient type and the participation constraint for the inefficient type in are the two relevant constraints for optimization.

77 These constraints are both binding at the second-best optimum, and so we have

$$U_L = U_H + \Phi(q_H) \text{ and } U_H = 0.$$

It leads to the following expression of the efficient type's rent

$$U_L = \Phi(q_H).$$

Since $\Phi' > 0$, reducing the inefficient agent's output also reduces, as before, the efficient agent's information rent.

78 Also, using the information rents and binding constraints, we can transform the principal's objective function from

$$\lambda \left[S(q_L) - C(q_L, \theta_L) \right] + (1 - \lambda) \left[S(q_H) - C(q_H, \theta_H) \right] - \left[\lambda U_L + (1 - \lambda) U_H \right]$$

to

$$\lambda \left[S(q_L) - C(q_L, \theta_L) \right] + (1 - \lambda) \left[S(q_H) - C(q_H, \theta_H) - \tfrac{\lambda}{1-\lambda} \Phi(q_H) \right].$$

79 With the assumptions made on C, one can also check that the principal's objective function is strictly concave with respect to outputs.

80 By ignoring θ_H-IC and the first order approach, optimal contract entails:

- No output distortion with respect to the first-best outcome for the efficient type, $q_L^{\text{SB}} = q_L^*$ with

$$S'(q_L^*) = C_q(q_L^*, \theta_L).$$

- A downward output distortion for the inefficient type, $q_H^{\text{SB}} < q_H^*$ with

$$S'(q_H^*) = C_q(q_H^*, \theta_H)$$

and

$$S'(q_H^{\text{SB}}) = C_q(q_H^{\text{SB}}, \theta_H) + \frac{\lambda}{1 - \lambda} \Phi'(q_H^{\text{SB}}).$$

- Only the efficient type gets a positive information rent given by $U_L^{\text{SB}} = \Phi(q_H^{\text{SB}})$.
- The second-best transfers are respectively given by $t_L^{\text{SB}} = C(q_L^*, \theta_L) + \Phi(q_H^{\text{SB}})$ and $t_H^{\text{SB}} = C(q_H^{\text{SB}}, \theta_H)$.

81 The first order conditions characterize the optimal solution if the neglected θ_H-IC is satisfied.

(a) For this to be true, we need to have

$$t_H^{\text{SB}} - C(q_H^{\text{SB}}, \theta_H) \geq t_L^{\text{SB}} - C(q_L^{\text{SB}}, \theta_H) = t_H^{\text{SB}} - C(q_H^{\text{SB}}, \theta_L) + C(q_L^{\text{SB}}, \theta_L) - C(q_L^{\text{SB}}, \theta_H),$$

which amounts to

$$0 \geq \Phi(q_H^{\text{SB}}) - \Phi(q_L^{\text{SB}}).$$

(b) Since $\Phi' > 0$, it is equivalent to $q_H^{\text{SB}} \leq q_L^{\text{SB}}$.

(c) We still have

$$q_L^{\text{SB}} = q_L^* > q_H^* > q_H^{\text{SB}}.$$

- $S'(q_L^*) = C_q(q_L^*, \theta_L) < C_q(q_L^*, \theta_H)$ because $C_{q\theta} > 0$. Hence, using the fact that $S(q) - C(q, \theta_H)$ is concave in q and maximum for q_H^*, we have $q_L^* > q_H^*$.
- $\Phi' > 0$ implies that $S'(q_H^{\text{SB}}) > C_q(q_H^{\text{SB}}, \theta_H)$. Thus, $q_H^{\text{SB}} < q_H^*$.

(d) So the Spence-Mirrlees property guarantees that only the efficient type's incentive constraint has to be taken into account.

Task

- Reading: 2.1–2.6 and 2.10 in [LM] (required), 14.C in [MWG] (required), 2.2–2.3 in [S] (optimal), 第 9 讲 in [聂] (required).

- Understanding:

    - 在逆向选择模型中，由于委托人与代理人之间的信息差异，可能对经济体的效率产生影响。
    - 这时，委托人需要设计合约，诱导代理人真实反映其类型，自发选择为其定制的合约。
    - 激励代理人这样做，是有成本的（即信息租金，与产出水平相关），从而无法实现完全信息时的最优结果，只能得到次优结果。
    - 其中的基本问题在于信息租金的抽取和配置的效率之间进行权衡和取舍。